

2023

(CBCS)

(6th Semester)

PHYSICS

ELEVENTH PAPER

(Thermal and Statistical Physics)

Full Marks : 75

Time : 3 hours

*The figures in the margin indicate full marks for the questions***(SECTION : A—OBJECTIVE)**

(Marks : 10)

Tick (✓) the correct answer in the brackets provided :

1×10=10

1. The velocity of a molecule increases with the rise in

- (a) pressure ()
(b) time ()
(c) kinetic energy ()
(d) temperature ()

2. The average kinetic energy associated with each degree of freedom is

- (a) kT ()
(b) $\frac{1}{2}kT$ ()
(c) $\frac{1}{3}kT$ ()
(d) $\frac{1}{4}kT$ ()

3. In thermal conduction of gas there is transport of

- (a) energy ()
(b) momentum ()
(c) mass ()
(d) particle ()

4. Maxwell's thermodynamic relation is

(a) $\frac{S}{T}_T = \frac{P}{V}_T$ ()

(b) $\frac{T}{V}_S = \frac{P}{S}_V$ ()

(c) $\frac{T}{P}_P = \frac{V}{P}_P$ ()

(d) $\frac{S}{T}_P = \frac{P}{V}_T$ ()

5. The relative probability between two different energy states having difference 1.1×10^{20} joules at 400 K temperature is

(a) e^1 ()

(b) e^2 ()

(c) e ()

(d) e^2 ()

6. Five particles are distributed in two phase cells. The number of macrostates is

(a) 6 ()

(b) 10 ()

(c) 32 ()

(d) $\frac{5}{2}$ ()

7. In canonical ensemble, there is fluctuation in

(a) matter only ()

(b) No fluctuation ()

(c) energy only ()

(d) both matter and energy ()

8. A collection of large number macroscopically identical but essentially independent system is

(a) phase space ()

(b) ensemble ()

(c) phase cell ()

(d) -phase ()

9. In Bose-Einstein distribution law, the particles of a system are identical and

- (a) indistinguishable ()
- (b) distinguishable ()
- (c) have zero velocity ()
- (d) have equal mass ()

10. Photons obey

- (a) M-B statistics ()
- (b) F-D statistics ()
- (c) B-E statistics ()
- (d) All of the above ()

(SECTION : B—SHORT ANSWER)

(Marks : 15)

Answer the following :

3×5=15

UNIT—I

1. What is mean free path? Write the expression for mean free path according to Maxwell.

OR

2. Calculate the root mean square velocity of a molecule of mercury vapour at 300 K. (Given, molecular weight of mercury = 221, $R = 8.3 \times 10^7$ joule/mole-K).

UNIT—II

3. What is thermodynamic function or potential? How many thermodynamic functions are there? Name them.

OR

4. Explain triple point with a labelled diagram. What is the value of F in triple point?

UNIT—III

5. Explain how β is related to temperature. What is the significance of β parameter?

OR

6. When a dice is thrown twice and obtain two numbers, what is the probability that these numbers are 6 and 4 precisely in that order?

UNIT—IV

7. Define ensemble. Write two uses of ensemble.

OR

8. Write a short note on microcanonical ensemble with the help of a labelled diagram.

UNIT—V

9. What is indistinguishability of particles? What role does it play in quantum statistics?

OR

10. What are fermions? Write the basic postulates of F-D statistics.

(SECTION : C—DESCRIPTIVE)

(Marks : 50)

Answer the following :

10×5=50

UNIT—I

1. (a) What is Brownian motion? Derive Einstein relation for Brownian motion. 6
- (b) Write any four postulates of kinetic theory of matter. 4

OR

2. (a) State and prove the law of equipartition of energy. 7
- (b) Obtain an expression for mean square velocity and root mean square velocity of a gas molecule. 2+1=3

UNIT—II

3. (a) Deduce an expression for the coefficient of viscosity (η). Explain the effect of temperature and pressure on the coefficient of viscosity. 5+3=8
- (b) Obtain the relation between coefficient of viscosity and coefficient of diffusion. 2

OR

4. (a) Derive the first and second TdS equation. 5
- (b) From the general expression of Maxwell's thermodynamical relations, deduce Maxwell's four thermodynamic relations. Use these relations to obtain $C_p - C_v = R$. 4+1=5

UNIT—III

5. (a) Define thermodynamic probability. Hence calculate the number of microstates for six particles to be distributed in two cells for macrostate (2, 4). 1+3=4
- (b) Mention the states or parameters that define the microstate of a system. 2
- (c) State and explain the postulate of equal a priori probability. Clarify the concept of a cell in a compartment. 2+2=4

OR

6. (a) What are the factors that specify the coordinate of a phase space? Show that the volume of a phase cell is given by $d\Omega = \frac{1}{h^3} d^3r d^3p$. 1+2=3

(b) Define the functions $\rho(E)$ and $\omega(E)$. Hence, show that from the relation between $\rho(E)$ and $\omega(E)$ for a single particle, $\rho(E)$ is directly proportional to \sqrt{E} . 1+3=4

(c) Starting with the relation between entropy and temperature, obtain the equation

$$S = k \log \Omega$$

Also, explain each symbol in the above equation. 3

UNIT—IV

7. (a) Derive the probability distribution function in a canonical ensemble. 5

(b) Compare the different properties among micro-canonical, canonical and grand-canonical ensembles. 4

(c) What do you mean by partition function? 1

OR

8. (a) Discuss the thermodynamic quantities in grand-canonical ensemble. Hence, derive an expression for entropy in terms of partition function. 4+2=6

(b) Explain Stirling's approximation in canonical ensemble. 4

UNIT—V

9. (a) Using Maxwell-Boltzmann distribution law, deduce the equation for—

(i) total internal energy and specific heat of an ideal gas at constant volume;

(ii) Maxwell-Boltzmann speed distribution law. 6

(b) Write any two limitations of Maxwell-Boltzmann method. 2

(c) How does F-D statistics differ from B-E statistics? 2

OR

10. (a) Write a short note on B-E distribution law. Derive an expression

$$n_i = \frac{g_i}{e^{\frac{\epsilon_i}{kT} + 1}}$$

for the most probable distribution of particle of a system obeying B-E statistics. 1+6=7

(b) What are Fermi energy and Fermi level? How does Fermi energy vary with temperature? 3
